

# Evaluation of Nonlinear Regional Stability Performance of Passenger Cars

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## ABSTRACT

With the development of automobile technology and the improvement of road facilities, the driving performance and driving environment of vehicles have been improved, and the speed of vehicles has accelerated. This also brings hidden dangers to vehicle safety. When the vehicle is driving under complex working conditions such as ice and snow roads or strong crosswind, the vehicle tends to be in a nonlinear area, and the vehicle is prone to instability due to drivers' insufficient driving experience and incorrect operation, resulting in traffic accidents and casualties and property losses. However, in the current evaluation system for passenger car safety, the performance of the linear region of the vehicle is mainly evaluated by limiting the maximum vehicle speed or lateral acceleration, and the stability of the nonlinear region of the passenger car is not comprehensively evaluated. This paper proposes a comprehensive evaluation index for passenger car safety based on stability and nonlinearity. The slowly increasing steer test under different speeds and different road conditions is conducted through the joint simulation of CarSim and MATLAB/Simulink, and the vehicle state can transition from the linear region to the nonlinear region under this test scenario, so the validity of the comprehensive evaluation index of passenger car safety proposed in this paper can be verified. The test results show that the index can quantitatively evaluate the safety of passenger cars under different test scenarios.

**Keywords:** Handling stability, Stability evaluation, Nonlinear region, Passenger car

## INTRODUCTION

Passenger car safety is often evaluated by handling stability. Vehicle handling stability not only affects the driving experience of the driver, but also guarantees the safety of vehicles at high speed. Therefore, vehicle handling stability testing has become a necessary test item in the process of vehicle development and has received wide attention from industry and academia. The research on vehicle handling stability can be traced back to the 1930s and can be divided into open-loop and closed-loop tests in terms of test forms; subjective evaluation, objective evaluation, and comprehensive evaluation in terms of evaluation methods (Bai et al. 2012; Lin, 2018; Zhong, 2019; Liu, 2021). So far, the steady static circular test (Gao, 2014), step steering test

(Yang et al. 2016), fish hook test (Sun, 2021), double lane change test (Chen and Guo, 2015), pylon course slalom test (Liu, 2017) and other tests have been proposed one after another. Objective evaluation indexes such as degree of understeer, steering sensitivity, maximum lateral acceleration, and yaw damping (Wang, 2012) and subjective evaluation means such as questionnaire (Wang, 2020) were constructed, and the correlation between subjective and objective evaluations was analyzed (Chen, 2016). At present, vehicle handling stability testing is often limited to a single test condition, failing to conduct a comprehensive analysis of the adaptability of evaluation indicators under different vehicle speeds, different road adhesion conditions and other working conditions. The evaluation index construction mainly focuses on evaluating the vehicle stability, describing the vehicle stability degree with qualitative or quantitative indicators, ignoring the nonlinear characteristics of the vehicle tends to destabilization process. Therefore, a comprehensive evaluation of vehicle stability and nonlinearity is expected to help the vehicle stability control system sense the destabilization trend in advance, correct the vehicle attitude in time, and avoid the vehicle losing the ability to be controlled as much as possible.

In summary, this paper intends to propose a comprehensive evaluation method for passenger car safety based on vehicle stability and nonlinearity. The slowly increasing steer test is chosen as validation experiment, in which the vehicle state can transit from the linear region to the nonlinear region, and by changing speed and road adhesion coefficient, the nonlinear state of the vehicle under different test conditions can be stimulated, and the adaptability of the comprehensive evaluation index to the test condition can be effectively evaluated. In the evaluation session, a comprehensive evaluation index is proposed considering the stability and nonlinearity of the vehicle state, characterizing the stability of the vehicle by the distance of the actual state from the safety boundary of the state, and characterizing the nonlinearity of the vehicle by the deviation between the actual state and the desired state of the vehicle, both of which are integrated as the comprehensive evaluation index of the vehicle. Finally, the validity of the comprehensive evaluation index proposed in this paper is verified by the joint simulation of CarSim and MATLAB/Simulink. On the one hand, this index can help to enrich the evaluation content of the handling stability in vehicle development, and on the other hand, it can provide the theoretical basis for the decision-making and control of autonomous vehicles.

## EXPERIMENTAL DESIGN

In order to promote the vehicle to reach the stability limit and enter into nonlinear state, the slowly increasing steer test is used as the validation experiment. The basic procedure of the validation test is as follows: the vehicle speed maintains constant. The steering wheel angle is incremented by 2deg/s, and the radius of curvature of the vehicle trajectory decreases as the steering angle increases. The vehicle state transits from the linear region to the nonlinear region, and finally the vehicle trajectory ends up in a spiral shape.

**Table 1.** Verification of comprehensive index under different road adhesion conditions.

Road friction coefficient	Velocity	Stop conditions
0.85	80km/h	The simulation time reaches 25s
0.6	80km/h	
0.4	80km/h	
0.2	80km/h	
	80km/h	

**Table 2.** Verification of comprehensive index under different velocity.

Road friction coefficient	Velocity	Stop conditions
0.2	100km/h	The simulation time reaches 25s
0.2	80km/h	
0.2	60km/h	
0.2	40km/h	

**Table 3.** Vehicle dynamics parameters table.

Parameter name	Numerical value
Vehicle mass(kg)	1860
Moment of inertia (kg·m <sup>2</sup> )	3438.5
Distance from centroid to front axle (m)	1.25
Distance from centroid to rear axle (m)	1.7
Centroid height (m)	0.72

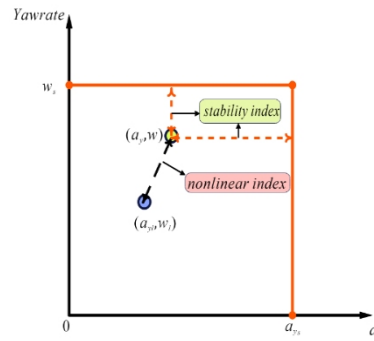
On this basis, considering that the vehicle speed and road adhesion conditions have a great influence on the vehicle stability and nonlinearity. To effectively stimulate the vehicle nonlinearity and further enrich the test content, slowly increasing steer tests are conducted under different vehicle speeds and different road adhesion conditions. The specific test settings are shown in Table 1 and Table 2.

In order to verify the performance of the proposed comprehensive evaluation index for passenger car safety, the Carsim and Simulink are used for joint simulation and the passenger car parameters in Table 3 are used.

### COMPREHENSIVE EVALUATION INDEX OF PASSENGER CARS

In this paper, we will evaluate the stability of the nonlinear region of passenger cars from these two aspects. In terms of vehicle stability characterization, considering the constraint of ground attachment on the vehicle state, this paper constructs a stability index to characterize the stability of the vehicle. In terms of nonlinear degree characterization, considering that the vehicle tends to deviate from the expected driving state when vehicle tends to be unstable, this paper constructs a nonlinear index based on the deviation between the actual state and the expected state of the vehicle to characterize the degree of nonlinearity.

Based on this, the key parameters required for the construction of the characterization index are shown in Figure 1. Where  $a_y$  is the actual lateral



**Figure 1:** Construction of comprehensive evaluation index.

acceleration, and  $w$  is the actual yaw rate, which can be measured by sensors or estimated (Xu, 2007; Bai, 2011; Chen, 2008).  $a_{ys}$  is the safety boundary value of lateral acceleration, and  $w_s$  is the safety boundary value of yaw rate.  $a_{yl}$  is the expected lateral acceleration and  $w_l$  is the expected yaw rate, which can be generated by driving data calibration or electronic stability controller such as ESP (Yu, 2017).

Vehicle is limited by the ground adhesion, and the yaw rate of the car should not be too large when driving at high speed, otherwise the vehicle is prone to dangerous behaviours such as sideslip. In this paper, the stability boundary of yaw rate and lateral acceleration are based on the road adhesion conditions (Hu, 2021), as shown in equation (1). The stability of the vehicle is characterized by calculating the maximum absolute value of the deviation between the actual state of the vehicle and the stability boundary under different conditions of the slowly increasing steer test, and each deviation term is normalized by the value of the stability boundary. The stability index is constructed as shown in equation (2). When the actual state of the vehicle is within the safe boundary value, the stability index is negative. As the vehicle state tends to the safety boundary, the tires tend to saturate and the stability index tends to 0. When the vehicle state is beyond the safety boundary range, the stability index is positive and the vehicle is prone to instability.

$$a_{ys} = 0.85 * \mu * g \quad (1)$$

$$w_s = \frac{a_{ys}}{V_x} \quad (2)$$

$$\text{Cos } t_s = \frac{|w|_{\max} - |w_s|}{|w_s|} + \frac{|a_y|_{\max} - |a_{ys}|}{|a_{ys}|} \quad (3)$$

When the vehicle is in good road conditions, the handling response will be more in line with driving expectations, but as the driving environment deteriorates, the tires tend to saturate and the degree of vehicle nonlinearity spikes. The response of yaw rate and lateral acceleration in the vehicle steering test can reflect the change of vehicle nonlinearity. In this paper, the vehicle nonlinear characteristics are characterized by the absolute maximum value of the deviation between the actual yaw rate and lateral acceleration of the vehicle

and the expected driving state value under different test conditions of the slowly increasing steer test, and the deviation term is normalized by the stable boundary value, which constitutes the nonlinear index as shown in equation (3). When the actual state of the vehicle is close to the expected value of driving, the nonlinear index tends to 0. As the nonlinearity of the vehicle increases, the value of the nonlinear index increases to a positive value.

$$\text{Cos } t_{nl} = \frac{|w - w_l|_{\max}}{|w_s|} + \frac{|a_y - a_{yl}|_{\max}}{|a_{ys}|} \quad (4)$$

The vehicle comprehensive evaluation index is a combination of stability index and nonlinear index, as shown in equation (4). The weight can be changed with the change of road attachment conditions. The side slip and other risk is not easy to occur on high adhesion road. The weight of nonlinear index in the comprehensive evaluation is higher on high road adhesion road, emphasizing the vehicle response state in line with driving expectations to avoid excessive response deviation leading to collision. The tires are easily saturated on low adhesion roads, and the vehicle is easily destabilized due to excessive driver tension or improper operation, so the stability index has a higher weight in the comprehensive evaluation process. When the comprehensive evaluation index is negative, it means that the nonlinearity of the vehicle is low, the nonlinear index tends to be close to 0, the actual state of the vehicle is far from the safety boundary value, and the stability of the vehicle is stronger. When the comprehensive evaluation index is positive, the vehicle nonlinearity degree is significant, and the actual state of the vehicle is close to or beyond the safety boundary value. At this time the wheels tend to saturate, and the vehicle is easy to destabilize.

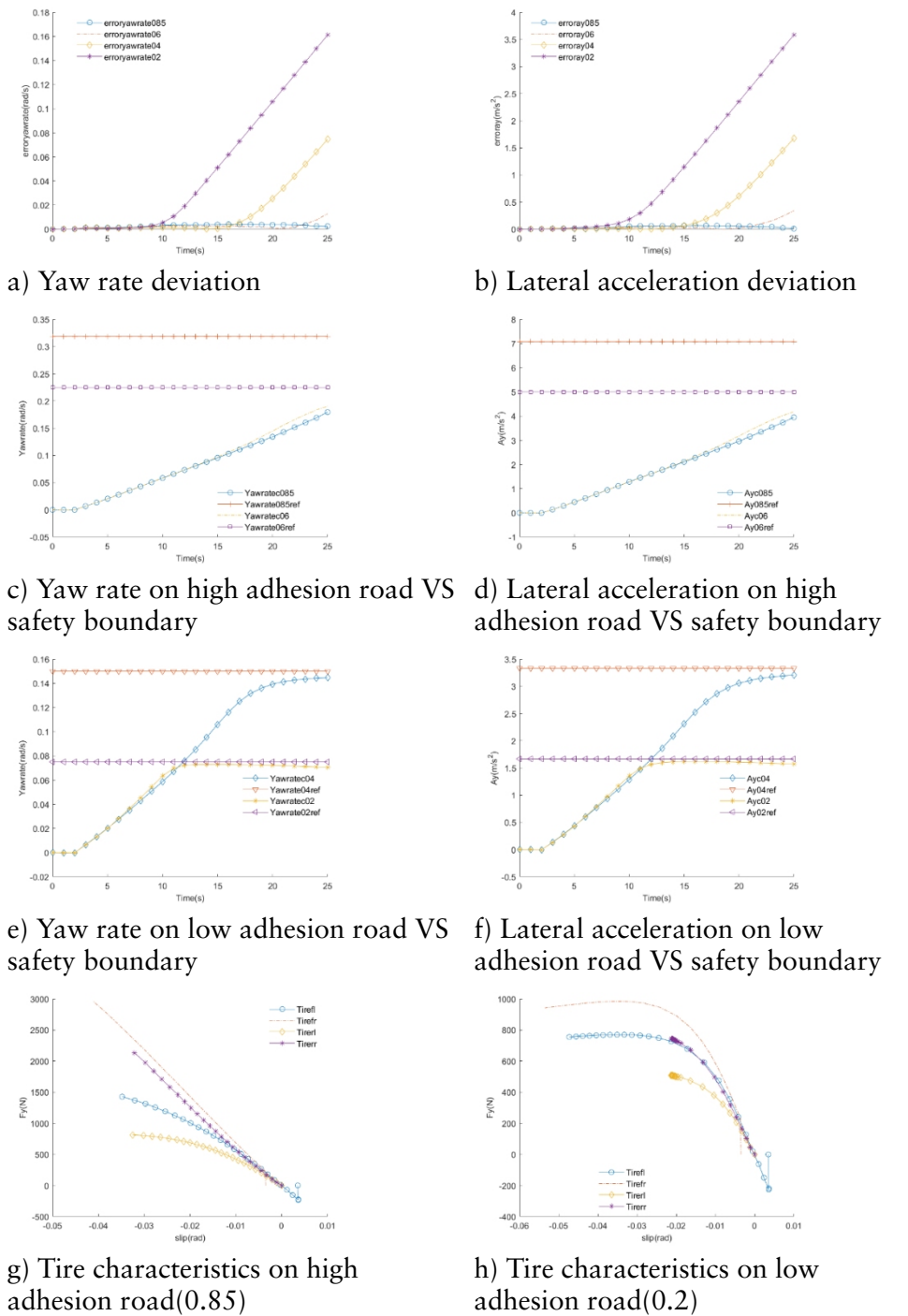
$$\text{Cos } t_{cs} = w_{st} * \text{Cost}_s + w_{nl} * \text{Cost}_{nl} \quad (5)$$

## RESULTS AND DISCUSSION

In terms of risk and repeatability, this paper uses simulation means to build a simulation environment through CarSim and Simulink, and conducts slowly increasing steer tests under different speeds and different road adhesion conditions to verify the comprehensive vehicle evaluation method proposed in this paper.

The results of the slowly increasing steer test under different road adhesion conditions are shown in Figure 2. As the road adhesion coefficient decreases, the wheels are more likely to reach the saturation state, so the degree of vehicle nonlinearity increases, and the deviation of the actual vehicle state from the desired state gradually increases. When the road adhesion coefficient is 0.4 and 0.2, the vehicle state value deviates more, and the nonlinearity is more obvious. The vehicle state is more biased to the safety boundary value, and the stability decreases.

The vehicle comprehensive evaluation index values under different road adhesion are shown in Table 3. It is not difficult to find that the index can effectively characterize the vehicle stability state differences under different road adhesion conditions. When road adhesion coefficient is 0.85 and 0.6,



**Figure 2:** Vehicle nonlinearity and stability characteristics under different road adhesion conditions.

the vehicle comprehensive evaluation index is negative. With the road adhesion coefficient reducing, its value tends to 0. When road adhesion coefficient is 0.2 and 0.4, the tire show saturation state, and its corresponding vehicle

**Table 4.** Comprehensive stability index under different road adhesion conditions.

Road friction coefficient	Velocity	Nonlinear index weight	Stability index weight	Comprehensive stability index
0.85	80km/h	0.6	0.4	-0.34
0.6	80km/h	0.6	0.4	-0.05
0.4	80km/h	0.4	0.6	0.36
0.2	80km/h	0.4	0.6	1.69

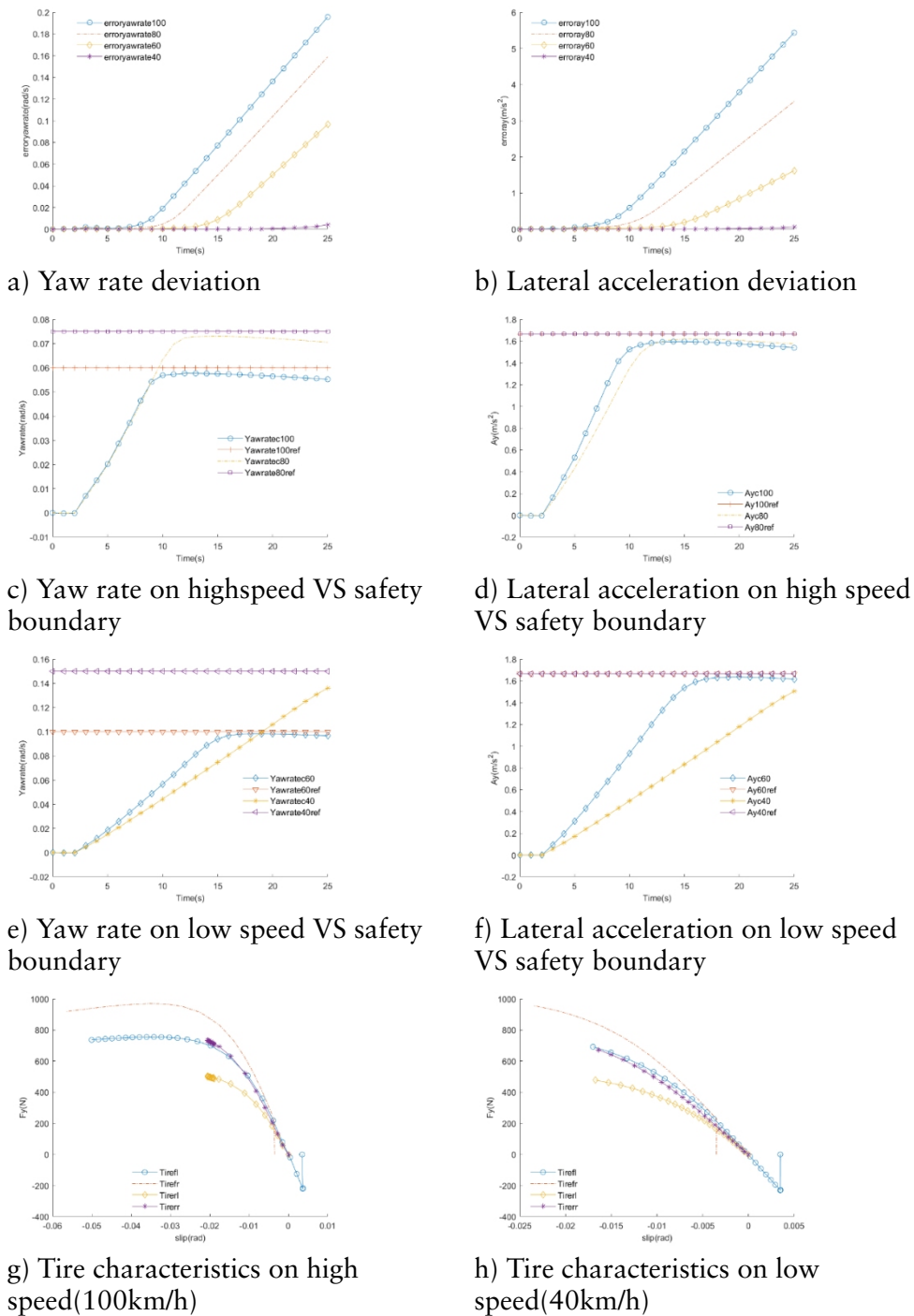
**Table 5.** Comprehensive stability index under different road adhesion conditions.

Road friction coefficient	Velocity	Nonlinear index weight	Stability index weight	Comprehensive stability index
0.2	100km/h	0.4	0.6	2.56
0.2	80km/h	0.4	0.6	1.69
0.2	60km/h	0.4	0.6	0.76
0.2	40km/h	0.4	0.6	-0.09

stability comprehensive evaluation index is positive. Meanwhile the vehicle nonlinear degree is significant, and the vehicle has seriously deviated from the expected state of driving. At this time, it is easy to cause the vehicle to collide with other vehicles in the process of obstacle avoidance due to understeering. In summary, under different road adhesion coefficient vehicle comprehensive evaluation index can effectively characterize the vehicle stability and nonlinearity degree.

The results of the slowly increasing steer test at different speeds are shown in Figure 3. As the vehicle speed decreases, the yaw rate deviation and lateral acceleration deviation decrease significantly, and the degree of vehicle nonlinearity is alleviated. When the vehicle speed decreases to 40km/h, the vehicle stability is improved. The wheels show significant saturation characteristics at high speed, and the vehicle nonlinearity is obvious, while the vehicle state is close to the safety boundary value. The vehicle is easy to lose control, and the driving risk is greatly increased.

It is not difficult to find that the index can effectively characterize the difference of vehicle stability state under different speed conditions. As shown in table 4, when the vehicle speed is 100km/h, 80km/h and 60km/h, the vehicle comprehensive evaluation index is positive, and the vehicle nonlinear characteristics are significant, and the value tends to 0 as the vehicle speed decreases. The comprehensive evaluation index transit to negative value when the speed decrease to 40km/h, and the degree of vehicle nonlinearity is improved more obviously. Therefore, it is an effective measure to reduce risk by decreasing speed appropriately when driving on the low adhesion road. In summary, the comprehensive vehicle evaluation index can effectively characterize the vehicle stability and nonlinearity at different speeds.



**Figure 3:** Vehicle nonlinearity and stability characteristics under different velocities.

**CONCLUSION**

In this paper, a feasible comprehensive evaluation method of vehicle stability and nonlinearity is proposed for passenger cars, including two aspects of test



design and evaluation index construction. The slowly increasing steer test is determined as the validation experiment, and the experimental conditions are extended to different vehicle speeds and different road adhesion conditions in order to effectively stimulate the vehicle nonlinearity. A comprehensive vehicle evaluation index consisting of stability index and nonlinearity index was constructed by considering the vehicle stability and nonlinearity degree. The adaptability of the comprehensive evaluation indexes to the changes of the test conditions is explored. Considering the risk and repeatability, the simulation means is selected to verify the validity of the vehicle comprehensive evaluation index. The simulation verification results show that, as the road adhesion coefficient decreases, the vehicle comprehensive evaluation index gradually changes from negative to positive values, while the vehicle stability decreases and the vehicle nonlinearity increases. At this time, reducing the vehicle speed is an effective measure. When the road adhesion coefficient is 0.2, the vehicle speed can be reduced to 40km/h to a certain extent to alleviate the vehicle instability trend, and the vehicle comprehensive evaluation index to return to negative values by decreasing speed. So that the comprehensive evaluation method proposed in this paper can not only effectively evaluate the difference of vehicle performance in linear and nonlinear regions, but also can quantitatively distinguish the difference of vehicle performance under different test conditions, and has certain robustness to both vehicle speed and road adhesion conditions. The evaluation method is expected to enrich the content of vehicle handling stability evaluation, and it can also empower the autonomous driving decision and control algorithm, and provide the theoretical basis for planning the corresponding safety measures for different working conditions. The weight of stability indicators and the weight of nonlinear indicators in the current comprehensive evaluation indexes are determined empirically, and the weight of relevant indicators should change adaptively due to the changing test scenarios in the actual driving of vehicles, so in the future research, the introduction of fuzzy algorithms is considered to realize the adaptive adjustment of comprehensive evaluation index weight values with the test scenarios.

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