

A Multimodal Approach to Predicting Toe Temperature: Experimental, CFD, and LSTM-Based Methods

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ABSTRACT

The assessment of footwear insulation in cold environments remains a challenge due to the lack of standardized evaluation methods beyond the pass/fail criterion of ISO 20344:2021. To address this gap, this study develops a multi-approach framework combining experimental measurements, computational simulations, and machine learning predictions to evaluate thermal protection in cold-weather footwear. Human trials were conducted in a controlled climatic chamber to examine thermoregulatory responses under varying environmental conditions, insulation levels, and activity intensities. To complement these measurements, computational simulations were performed to estimate the thermal resistance (R_{cT}) of footwear under ISO 15831:2004 conditions. Additionally, a Long Short-Term Memory (LSTM) neural network was trained on experimental data to predict big toe temperature based on skin temperature, ambient conditions, and activity levels. This integrated approach enables a more comprehensive evaluation of footwear thermal performance, providing valuable insights for footwear manufacturers and researchers.

Keywords: Machine learning, CFD, Human thermoregulation, Thermoregulation model

INTRODUCTION

Cold protection shoes are a complex system. They are made of many different materials and even in the sports field, they are considered more closely as personal protective equipment (PPE) rather than casual sportswear. Today, there is no reliable standard to assess and correctly differentiate between the various insulation levels of different shoe models. The only existing standard is ISO 20344:2021 (ISO 20344, 2021), which was developed for work environments. However, it only relies on a pass/fail criterion, which brings with it some limitations, such as a deceptive sense of security, a complete lack of distinction between different levels of insulations, and a lack of evaluation of protection in practice (Kuklane et al., 2009).

Especially in cold environments, thermoregulation of the extremities (such as hands and feet) works differently from that of the whole body. It is affected by mechanisms such as vasoconstriction and cold-induced vasodilation, which in some extreme cases can lead to severe hypothermia and frostbite. In the literature, some studies have been carried out to observe

how thermoregulation works on feet (Bianca et al., 2024; Kuklane, 2009; Taylor et al., 2014; Zhang et al., 2024) and it has been found that a crucial condition for feet health that appears at 15 °C. In this situation, pain receptors take precedence over the cold receptors and if this temperature is maintained for a prolonged period, tissue death may occur.

As it is important to improve the evaluation of the thermal properties of highly technical footwear (e.g., mountain boots for alpinism and extreme expeditions) in the sports sector, two parameters have been developed in this work with the purpose of allowing the manufacturer to more deeply explore and compare the performance different prototypes in their intended environmental conditions. The first approach is concerned with predicting (using a Neural Network, NN) the maximum duration of exposure (in time, hours) a person could be in the environmental conditions under consideration when wearing the specified insulation before reaching the 15 °C threshold for the big toe. The second parameter is the estimation of R_{cT} (m^2K/W) for new prototypes of footwear thanks to the development of a CFD model in which the test conditions of ISO 15831:2004 (Clothing - Physiological effects. Measurement of thermal insulation by means of a thermal manikin) (ISO 15831, 2004), were reproduced.

METHODOLOGY

Experimental Tests

Human tests were carried out to observe human thermoregulation in different scenarios (all considering cold and hostile environments). The tests were carried out in a climate chamber at the Polytechnic University of Turin and at Loughborough University. The factors that had the greatest impact on human thermoregulation were clothing insulation, environmental conditions (such as temperature and wind speed), and the level of physical activity. For this reason, the tests were carried out in such a way that one characteristic was varied per test. To summarise, the different protocols were carried out as follows:

- Simulated mountaineering excursions: Participants were exposed to different environmental conditions (−10 °C, −15 °C, −17 °C, −20 °C, −30 °C) wearing two different insulation levels of footwear (with different clo values where 1 clo corresponds to 0.155 m^2K/W) to simulate real mountaineering activities.
- Light walking exercises on a treadmill: Participants walked lightly to maintain a sufficient metabolic rate and avoid shivering. Shivering is unwanted in these tests as its connected metabolic response would constitute a confounding factor. The tests were carried out under different environmental conditions (−10 °C, −15 °C, −17 °C, −20 °C, −30 °C) and with different insulation levels of the boots (clo value).
- Worst-case scenario tests: Participants were asked to remain in the climate chamber, where extreme conditions were simulated, with different environmental conditions (−10 °C, −15 °C, −17 °C, −20 °C, −30 °C) and different levels of footwear insulation (clo).

In each test, some parameters were determined, such as mean skin temperature, which was assessed using the 14-point method described in the international standard ISO 9886:2004 (Ergonomics - Assessment of thermal strain by physiological measurements) (ISO 9886, 2008), the temperature of the big toe, the heart rate, the levels of insulation of the different garments worn, which were assessed according to ISO 15831:2004, and thermal images to assess the surface temperature of the boots and to define the cleats that were effectively in contact with the ground.

Computational Models

Starting from an existing model of boot designed for extreme alpinism and ice climbing (Phantom Tech HD, produced by S.C.A.R.P.A., Asolo, Italy) a 3D reconstruction was created with CAD software. According to the different areas in terms of composition, the model was split into eleven regions to allow the user to assign different thermal properties according to the subjected area. For this purpose, the materials involved were tested according to ISO 9920:2007 (Ergonomics of the thermal environment — Estimation of thermal insulation and water vapor resistance of a clothing ensemble) (ISO 9920, 2007) to evaluate their thermal properties. A User Defined Database (UDD) was created as a material library. Numerical simulations were set up in Computational Fluid Dynamics (CFD) software to reproduce the same test condition of the ISO 15831:2004 standard. For this reason, the internal volume of the boot structure is constituted by a hot body set at a T_{foot} of 34 °C. Gaps of quiescent air were interposed between the boot and the “body” in some specific areas (i.e., the lacing area and the contact area between the foot and the insole were excluded supposing a perfect contact in these areas) to mimic the realistic presence of an air layer in the system. The ambient temperature (T_a) was set to 10 °C and different boundary conditions were imposed in the different areas of the boots:

- Heat transfer coefficient: in the areas in which the boot was in contact with the layer of quiescent air, a convective boundary condition was imposed using a convective heat transfer coefficient (h_c) calculated with T_a and a wind speed (w_s) of 0.4 m/s as specified in the reference standard. The h_c was then evaluated as follows (Parsons, 2014; Santee and William, 2012):

$$h_c = \frac{Nu \cdot k_a}{L} \text{ (Wm}^{-2}\text{K}^{-1}\text{)}$$

Where Nu is the Nusselt number, k_a is the thermal conductivity of air and L is the characteristic length (set as a constant at a value of 0.4 m). Nu was evaluated as (Parsons, 2014):

$$Nu = 0.24 \cdot Re^{0.6}$$

Re is the Reynolds number given by the ratio between the product of w_s and L and the kinematic viscosity of air at the temperature considered, denoted ν (i.e., $1,31 \cdot 10^{-6} \text{ m}^2\text{s}^{-2}$ at 10 °C).

The value of k_a was calculated with the following method (Kerslake, 1972):

$$k_a = 2.41 \cdot 10^{-2} + 7.8 \cdot 10^{-5} \cdot T_a \text{ (Wm}^{-1}\text{K}^{-1}\text{)}$$

T_a is the ambient temperature in K.

- Prescribed temperature: in the area in which the boot was in contact with the ground a fixed temperature was imposed at the same value of T_a . The cleats that effectively were in contact were observed with the thermal images acquired in the experimental campaigns. The same condition was set in the hot body, fixing his temperature at T_{foot} .

In this way, the value of the R_{cT} of the boot was calculated, and the ratio between the temperature gradient between the foot and the environment and the heat flux released by the hot body to keep its temperature constant as follows:

$$R_{cT} = \frac{(T_{\text{foot}} - T_a)}{H_{f,\text{foot}}} \text{ (m}^{-2}\text{K/W)}.$$

Data-Driven Model

Due to the strong correlation between mean skin temperature and big toe temperature, various approaches have been explored to predict big toe temperature from skin temperature data. Given the strong temporal dependencies in the dataset, the most effective approach identified relies on Recurrent Neural Networks (RNNs). However, a major challenge with these architectures is the vanishing gradient problem: during backpropagation through time (BPTT), gradients can shrink exponentially, leading to near-zero weight updates and the loss of long-term dependencies.

This issue has been effectively addressed with the introduction of Long Short-Term Memory (LSTM) networks, which differ from standard RNNs by incorporating an internal recurrence (self-loop). This mechanism helps regulate the flow of information and mitigates the effects of vanishing and exploding gradients (Lipton et al., 2015; Mienye et al., 2024). Specifically, each LSTM cell includes additional parameters and a system of gating units—input, output, and forget gates—that dynamically control information retention and forgetting, allowing the network to selectively propagate relevant information while discarding less important signals. The neural network was trained on the datasets collected from human experiments. The data were labeled based on the following criteria: temperature (ambient temperature at which the tests were conducted), activity level (0 for rest, 1 for light walking, and 2 for intense activity), and R_{cT} (insulation level of the boot worn). Before training, the dataset was normalized using a Robust Scaler to ensure consistent feature scaling. Furthermore, hyperparameter tuning was conducted to optimize the model's performance. The parameters adjusted included: the number of units in the first and second LSTM layers, dropout rates for both layers, and the learning rate. Moreover, a custom loss function to monitor the training process was created to evaluate the algorithm

performance based on the difference between the predicted time to reach the threshold and the experimentally measured one.

Once the LSTM was trained, the prediction of big toe temperature was compared with the test datasets (one for each condition) previously excluded from the training and validation ones (splitting of the training dataset in training and validation was done at 20%). The final, most robust, LSTM was then used as a big toe temperature predictor, which uses as input the mean skin temperature given by the thermoregulation model JOS-3 (Choudhary and Udayraj, 2023; Kobayashi and Tanabe, 2013; Takahashi et al., 2021).

RESULTS

The most accurate Long Short-Term Memory (LSTM) architecture, as identified through hyperparameter optimization, consisted of the following configuration:

- Two LSTM layers followed by a final dense output layer.
- Number of units in the first layer: 128.
- Number of units in the second layer: 32.
- Dropout rates: 0.4 (first layer), 0.2 (second layer).
- Learning rate: $1e-5$.
- Optimizer: Adam.
- Activation function: *tanh* for both LSTM layers.

Figure 1 presents a surface plot of the mean absolute error (MAE, evaluated as the distance between the predicted and true temperature time series) on the validation set across all tested hyperparameter configurations, presented as a function of only two of the five explored hyperparameters in each subplot. The effect of changing the number of layers, type of optimizer, and activation function is not shown as the presented choices were quickly identified as the best ones without the need of a structured optimization approach. To ensure clarity in the visualization, only the top 50 performing configurations are displayed.

A custom loss function was also implemented to better reflect the specific prediction objective. Since the primary goal of the model is to estimate the time at which the temperature curve reaches a critical threshold of 15 °C, the loss function incorporates a SoftMax component that penalizes discrepancies between the predicted time-to-threshold and the experimentally observed value. The β parameter of the SoftMax function, which controls its sharpness, was also tuned as part of the optimization process.

The model's predictions were evaluated against experimental data in six different scenarios. As illustrated in Figure 2, prediction accuracy tends to degrade in scenarios labeled as Level 2 physical activity (i.e., high-intensity exertion). This reduction in performance may be attributed to inter-individual variability in physiological response to intense activity due to different training levels, which introduces additional complexity to the prediction task.

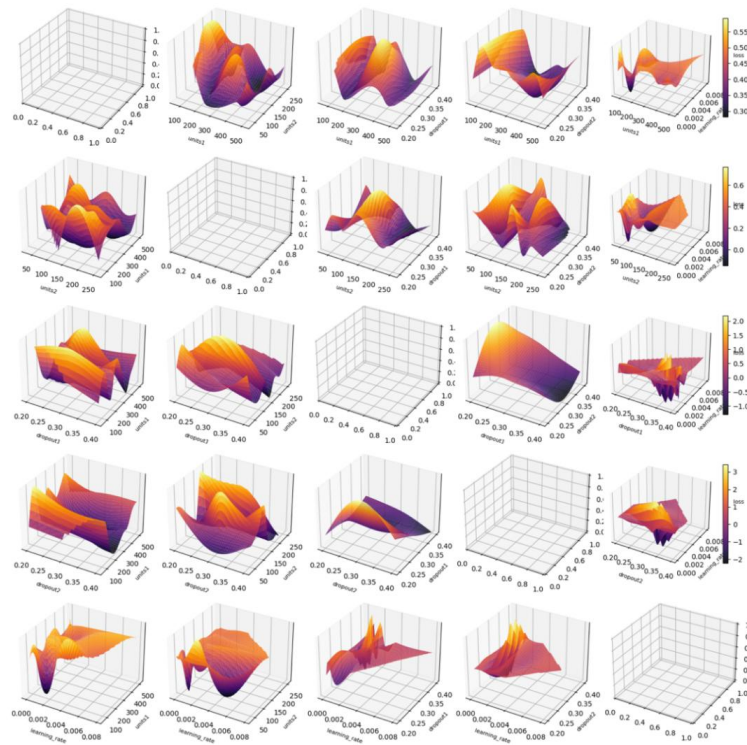


Figure 1: Surface plot of the best 50 architectures resulting from the hyperparameter tuning.

Despite this, the LSTM model performs well under “critical” scenarios—such as conditions involving sustained stillness for 70 minutes—demonstrating its robustness in predicting temperature dynamics under thermally stressful but physically passive conditions.

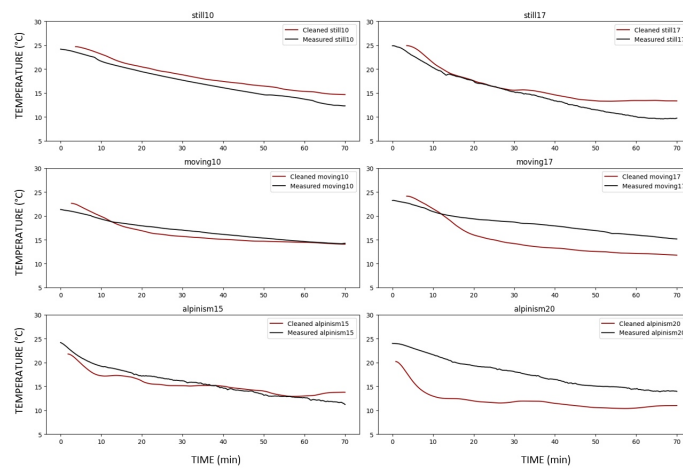


Figure 2: Comparison between test and predicted data.

In Table 1 the performance in terms of accuracy of the predicting the time to reach threshold (i.e., 15 °C) is reported. The different scenario is labelled as (ambient temperature, level of activity, and level of boot insulation) where the level of boot insulation is defined as A or B. The model's predictions were evaluated based on the following classification (Heydarian et al., 2022): True Positive (TP) if the threshold was reached within ± 10 minutes of the experimental time, False Positive (FP) if the prediction deviated by more than 10 minutes from the experimental time, True Negative (TN) if neither the prediction nor the experimental curve reached the threshold, and False Negative (FN) if the error exceeded 10 minutes.

Based on the confusion matrix in Table 1, the model results in the following:

- TP = 3.
- FP = 2.
- TN = 0.
- FN = 1.

Then, the accuracy, precision, and recall are evaluated as follows:

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

$$Precision = \frac{TP}{TP + FP}$$

$$Recall = \frac{TP}{TP + FN}$$

Table 1: Confusion Matrix of the LSTM model.

Case	Ground Truth	LSTM Prediction	Time Error (min)
(−10, 0, A)	1	1	2
(−17, 0, B)	1	1	6
(−10, 1, A)	1	1	10
(−17, 1, A)	1	0	N/A
(−15, 2, B)	1	1	5
(−20, 2, B)	1	1	30

The accuracy measures the proportion of correct predictions over the total number of cases, providing an overall indication of model performance. Precision represents the ratio of true positives to the total number of predicted positives, reflecting the correctness of positive predictions. Recall measures the ratio of true positives to the total number of actual positives, indicating the model's ability to correctly identify positive cases.

The model achieved an accuracy of 0.5, precision of 0.6, and recall of 0.75. These results indicate that while the model is relatively effective at identifying instances where the temperature crosses the 15 °C threshold, it also experiences some significant prediction errors.

The high recall (75%) suggests that the model successfully identifies most of the positive cases—when the temperature drops below 15 °C. However, the lower precision (60%) indicates that the model incorrectly predicts some events, resulting in false positives. This suggests that the model is more adept at identifying potential threshold crossings but tends to overestimate their occurrence in some cases. The accuracy value of 50% reflects that the model makes correct predictions in only half of the cases. This could be attributed to a high error rate in both positive and negative classifications, possibly influenced by class imbalance or the inherent difficulty of the prediction task. These results highlight the trade-off between precision and recall, which is common in classification problems. In this case, prioritizing recall over precision has led to a model that detects more positive events but at the cost of increased false positives.

Moreover, the development of a standardized system for CFD simulations has significantly enhanced the model's predictive capabilities. By simulating thermal dynamics in various boot configurations, the model can now predict the temperature decrease over time under different environmental and physical activity conditions. The CFD simulations are particularly valuable in estimating the R_{cT} of new boot models, which is one of the key parameters used by the neural network to make predictions.

The reliability of the CFD system has been rigorously evaluated by comparing the simulation results with experimental data. Specifically, the deviation between the simulated R_{cT} values and those obtained through laboratory tests, conducted according to the ISO 15831 standard, was analyzed.

This comparison ensures that the CFD model accurately reflects the real-world performance of different boot models, thereby validating its use in the overall prediction process.

CONCLUSION

A new method for monitoring and predicting the physiological response in terms of thermoregulation in cold environments, specifically concerning the monitoring of big toe temperature, has been developed. Future improvements could involve fine-tuning the model to strike a better balance between these two metrics, potentially by adjusting the classification threshold or exploring additional techniques for handling class imbalance. Although the model currently operates with a slight bias toward false positives, it is preferable to adopt a more conservative approach in this context. Since the goal is to predict and avoid hazardous conditions, prioritizing the detection of potential threats, even at the cost of increased false positives, ensures a safer outcome, as it helps to prevent dangerous situations before they occur.

CONFLICT OF INTEREST

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